The Relational Model & Relational Algebra

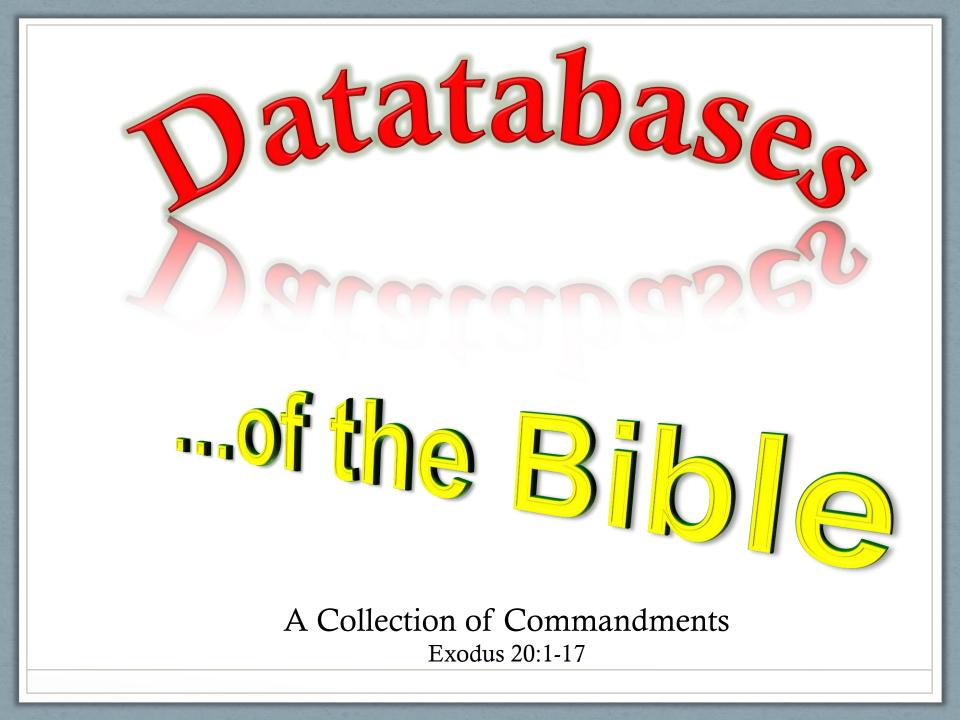
CPS 352: Database Systems

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Agenda

- Check-in
- The Relational Model
- Design Project Requirements Presentations
- Relational Algebra
- Homework 1





The Relational Model

Databases Have a History.

- Hierarchical and network databases came first
- First relational databases pioneered in 1970s
 - Simpler than earlier models (easier for programmers)
 - Based on mathematical theory of relations (expressed via relational algebra).
 - Had performance issues which helped other models to persist for a time
 - Extensive research (i.e. on indexing strategies) helped overcome performance bottlenecks
- Today, the relational model is dominant in the database world
 - Though other approaches are often used in tandem with it *polyglot persistence*

Databases Have Entities and Relationships.

- All database models must implement the following two concepts
 - *Entity* real or abstract "things"
 - *Relationships* between entities
- Relational model represents both entities and relationships via *tables*.
 - Table *attributes* (columns) must be *atomic* and *single valued*

Mathematical Terminology

- *Relational database* a collection of relations
- *Relation* a set of *tuples* of some *arity*
 - *Tuple* -- a record in the set
 - *Arity* number of component *attributes* in a tuple
 - Tuples in any given relation have the same arity
 - Order of attributes in tuples is important
 - Order of tuples in relation is not important
- *Attribute* numbered or named component of a tuple
 - Drawn from a specific domain or set of possible values
- *Relation scheme* structure of tuples in a relation
- *Instance* a specific relation on some scheme
 - Subset of the *Cartesian product* of the domains of its attributes

Alternative Terminology

Mathematical

- Relation
- Tuple
- Attribute
- Relation scheme

Alternate

- Table
- Row
- Column
- Sometimes represented by column headings

Tuples are Uniquely Identified by Keys.

- The tuples comprising a relation must be unique
 - No duplicates because the relation is a set
- *Superkey* Set of attributes which distinguish any tuple in the relation from all others
- *Candidate key* a superkey with no proper subset of attributes that is also a superkey
- *Primary key* a candidate key chosen to be the basis for uniquely identifying tuples
 - Underlined in a relation definition.
- *Foreign key* column(s) in one table that comprise the primary key of another table
 - Represent relationships in a relational database

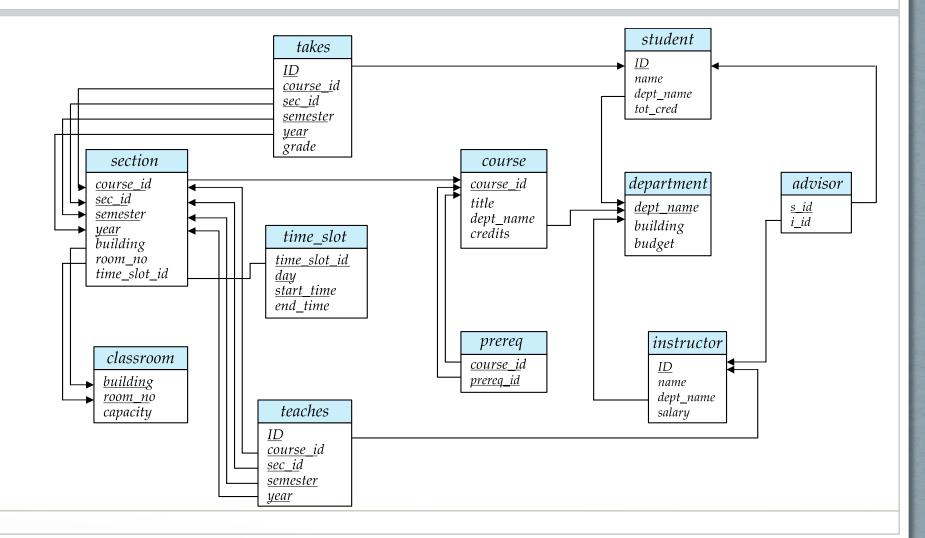
Nulls are for Missing on Undefined Attribute Values.

- Special value NULL assigned to a field when the attribute's value is unknown or does not exist
- NULL is not the same as:
 - String of spaces (" ")
 - Empty string ('')
 - Zero (0)
 - NULL (NULL = NULL even returns false)
- Databases can specify not null constraints on columns which must have values
 - i.e. Candidate, primary, and foreign key columns

Schemas and Instances

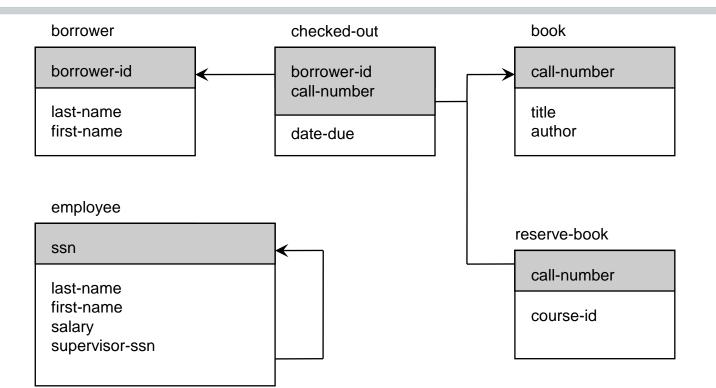
- *Schema* the logical design of a database
 - Database schema comprised of tables (relations) and their relationships with one another
- *Instance* a snapshot of the actual data (relations) in the database at a given point in time
- Schema diagram depicts entities and relationships in a database schema
 - Primary keys shaded or underlined
 - Foreign keys represented by arrows between related tables

University Schema Diagram



Design Project Requirements Presentations

Library Schema Diagram



Simplifying assumptions for this example:

- 1) author of a book is single-valued
- 2) there is only one copy of a book with a given call number
- 3) a given book can only be on reserve for a single course
- 4) course-id is presumably a foreign key in a table not shown

Example Library Instance

borrower(<u>borrower_id</u> , last_name, first_name)							
12345 20147	aardvark cat	anthony charlene					
89754	dog	donna					
60984 54872	fox zebra	frederick zelda					
book(<u>call number</u> , title, author)							
	Wenham Zo	· ·		elephant			
RZ12.905	5	ts I Have Knov	vn	dog			
LM925.04	· · · · · · · · · · · · · · · · · · ·	Cook a Cat	dog				
AB123.40	Karate	aall muml	oor dat	koala dua)			
checked_out(borrower_id, call_number, date_due)							
89754	RZ12.905						
89754		2002-11-10					
20147	AB123.40	2002-11-15	1)				
reserve_book(<u>call_number</u> , course_id)							
QA76.093	BY123						
AB123.40	PE075						
employee(<u>ssn</u> , last_name, first_name, salary, supervisor_ssn)							
123-45-6789	aardvark	anthony	40000	null			
567-89-1234		boris	30000	123-45-6789			
890-12-3456	-	emily	50000	123-45-6789			
111-11-1111	fox	frederick	45000	567-89-1234			

Example Queries Against the Library Database

- What is the name of the borrower whose borrower id is 12345?
- List the names of all borrowers.
- What is the title of the book whose call number is QA76.093?
- List the titles of all books that are currently checked out.
- List the names of all borrowers having one or more books overdue.
- List the names of all employees who earn more than their supervisor.
- List the names of all people connected with the library whether borrowers, employees, or both.

- List the names of all borrowers who are not employees.
- List all books needed as course reserves that are currently checked out to someone.
- List the names of employees together with their supervisor's name.
- List the call numbers of all overdue books, together with the number of days they are overdue.
- What is the average salary of all employees?
- Print a list of borrower id's and the number of books each has out
- List the titles of all books, together with the borrower id of the person (if any) who has the book out.

Query Languages

- All DBMS's support at least one query language which allow for the following
 - Interactive usage
 - Ability to embed within applications in programming languages
- Classifications
 - Formal query language uses mathematical notation and concepts useful for research (i.e. proving theorems)
 - Relational algebra
 - Commercial languages built on top of mathematical language principles for easier usage
 - SQL

Relational Algebra

Relational Algebra Operations

- Involve either one or two relations
 - Unary and binary operations
- Each operation returns a new relation
 - Enables composing or "chaining" of relations
- Operation Types
 - Primitive Operations
 - Composite Operations
 - Built with primitive operations, but common enough to warrant their own operations
 - Extended Relational Algebra

Primitive Operations

- Selection
- Projection
- Join a.k.a. Cartesian Product or Simple Join
- Rename
- Union
- Difference

Selection Retrieves Rows.

- Select rows/tuples from a table/relation which meet certain criteria
- Denoted by lowercase Greek letter sigma -- σ
- Example: What is the name of the borrower whose borrower id is 12345?
- $\sigma_{borrower_{id} = 12345}$ borrower
- Returns: 12345, aardvark, anthony
 - A subset of rows/tuples in a table/relation
- Multiple criteria can be specified by logical operators
 - ∧ and
 - V -- or
 - – -- negation (not)

Projection Chooses Columns

- Choose only specific columns/attributes from all rows/tuples in a table/relation
- Denoted by the lowercase Greek letter pi π
- Example: List the names of all borrowers
- π_{last_name, first_name} borrower
- Returns the following rows/tuples
 - aardvark, anthony
 - cat, charlene
 - dog, donna
 - fox, frederick
 - zebra, zelda

Relational Algebra Operations can be Combined.

- Relational algebra operations can be combined
- Example: What is the title of the book whose call number is QA76.093?
- $\pi_{\text{title}} \sigma_{\text{call_number} = QA76.093} \text{ book}$
- Returns: Wenham Zoo Guide

Projection and Duplicate Results

- A projection could produce duplicate rows by suppressing the column(s)/attribute(s) which distinguish rows.
- Example: List authors of books
- π_{author} book
 - This is a problem
- Duplicates eliminated because relations are sets
- Returns the following
 - dog
 - elephant
 - koala

Cartesian Product / Simple Join Fetches all Row Combinations

- Select every combination of rows/tuples from two tables relations
 - Result has as many rows as the product of the number of rows/tuples in the two tables/relations being joined
 - Result has as many columns/attributes as the sum of the columns in each table/relation involved in the join
- Denoted by a capital X

Cartesian Product Example

- Example: List the titles of all books that are currently checked out
 - Requires an initial Cartesian product
- checked_out X book

Borrower call id number	date-due call number	title	author
89754 RZ12.90	5 11-10-02 QA76.09	93 Wenham Zoo Guide	
elephan	t		
89754 RZ12.90	5 11-10-02 RZ12.90)5 Fire Hydrants I Have Known	dog
89754 RZ12.90	5 11-10-02 LM925.0	04 21 Ways to Cook a Cat	dog
89754 RZ12.90	5 11-10-02 AB123.4	10 Karate	koala
89754 LM925.0	4 11-10-02 QA76.09	93 Wenham Zoo Guide	
elephan	t		
89754 LM925.0	4 11-10-02 RZ12.90)5 Fire Hydrants I Have Known	dog
89754 LM925.0	4 11-10-02 LM925.0	04 21 Ways to Cook a Cat	dog
89754 LM925.0	4 11-10-02 AB123.4	10 Karate	koala
20147 AB123.4	0 11-15-02 QA76.09	93 Wenham Zoo Guide	
elenhan	+		

Cartesian Product Example (continued)

- Apply selection to limit results to meaningful rows/tuples
 - $\sigma_{checked_out.call_number = book.call_number}$ (checked_out X book)

• Yields the following:

 89754
 RZ12.905 11-10-02 RZ12.905 Fire Hydrants I Have Known
 dog

 89754
 LM925.04 11-10-02 LM925.04 21 Ways to Cook a Cat
 dog

 20147
 AB123.40 11-15-02 AB123.40 Karate
 koala

- Use a projection to return only book titles
 - $\pi_{\text{title}} \sigma_{\text{checked_out.call_number} = \text{book.call_number}}$ (checked_out X book)
- Which in turn yields:
 - Fire Hydrants I Have Known
 - 21 Ways to Cook a Cat
 - Karate

Rename Changes the Names of Tables and Columns.

- Renames a given table/relation and potentially its attributes as well
- Denoted by the lowercase Greek letter rho ρ
- Useful in conjunction with joins
 - Especially when joining a table with itself
- Example: List the names of all employees who earn more than their supervisor
- $\pi_{employee.last_name, employee.first_name} \sigma_{employee.supervisor_ssn = supervisor.ssn \land employee.salary > supervisor.salary (employee X <math>\rho_{supervisor}$ employee)
- Returns
 - elephant, emily
 - fox, frederick

Union "Stacks" Rows from Multiple Similar Tables.

- Combine two tables/relations in the same scheme into one
 Eliminates duplicate rows/tuples
- Denoted by U set algebra operator
- Example: List the names of all people connected with the library whether borrowers, employees, or both
- ($\pi_{last_name, first_name}$ borrower) U ($\pi_{last_name, first_name}$ employee)
- Preparing similar tables/relations for union operation
 - Projecting columns/attributes common to both relations
 - Renaming attributes

Difference "Subtracts" Rows in One Table from Another Table

- Takes rows/tuples from two tables/relations with the same scheme, and returns only those rows present in the first table, but not the second
- Denoted by set algebra operator
- Example: List the names of all borrowers who are not employees.
- (π_{last_name, first_name} borrower) (π_{last_name, first_name} employee)

Composite Operators

- Intersection
- Natural Join
- Theta Join
- Semijoin
- Antijoin

Intersection Returns Rows Common to Multiple Tables.

- Returns rows/tuples from two tables/relations with the same scheme which occur in both of them
- Denoted by \cap set algebra operator
- Example: List all books (call numbers only) needed as course reserves that are currently checked out to someone
- ($\pi_{\text{call_number}}$ reserve_book) \cap ($\pi_{\text{call_number}}$ checked_out)
- Can be computed via primitive relational operations
 - Given relations R and S:
 - Intersection = R (R S)

Natural Join Retrieves Matching Rows Using Shared Column Value.

- Special join which returns only those rows/tuples from two tables/relations which have the same values in one or more columns/attributes in a selection
 - Natural join removes duplicate join key values
- Denoted by the |X| (bowtie) operator
- Example: List all data for books that are checked out
 book |X| checked_out
- Same as this.
 - $\begin{array}{l} \pi & \mbox{checked_out.call_number, borrower_id, date_due, title, author} \\ \sigma & \mbox{checked_out.call_number} = \mbox{book.call_number} \ (\ checked_out \ X \ book \) \end{array}$
 - Based on Cartesian product

Theta Join (θ-join) Returns Matching Rows Using Comparisons.

- Join allowing for any arithmetic comparison operator (<, ≤, =, ≥, or >), not just strict equality of values of columns/attributes
 - Natural join (which does an equality comparison) could actually be a subset of theta join
 - Sometimes referred to as an equijoin
- Example: List the names of all employees together with their supervisor's name
 - Can be done as follows:
 - Cartesian product of the table against itself (renamed appropriately)
 - Selection comparing the employee's and supervisor's SSN values
 - Projection of the desired name data
 - $\begin{array}{c} \pi \\ e.last_name, \ e.first_name, \ s.last_name, \ s.first_name, \ s.first_name, \ s.first_name, \ \sigma \\ e.supervisor_ssn = s.ssn \ (\ \rho \ e \ employee \ X \ \rho \ s \ employee \) \end{array}$
- The selection can be "injected" into the Cartesian product as its join criteria for improved efficiency
 - $\begin{array}{c} \pi_{e.last_name, \ e.first_name, \ s.last_name, \ s.first_name} \ employee \\ (\rho_{e} \ employee \ X_{\theta \ e..supervisor_ssn \ = \ s.ssn} \ \rho_{s} \ employee) \end{array}$

Semijoin Returns Natural Join Matches from One Relation.

- Does a natural join and returns attributes from just one of the relations.
 - Left (|X) and right (X|) semijoins
- Example: For book |X| checked_out
 - Left semijoin (book |X checked_out) returns call_number, title, and author attributes
 - Right semijoin (book X | checked_out) returns borrower_id, call_number, date_due)

Antijoin Yields Records without Matches.

- Returns tuples that are not in the natural join results
- Denoted by \Box operator
- Example: List data on books that are not checked out.
 - books □ checked_out
 - Same as this:
 - books (books |X| checked_out)

Extended Relational Algebra

- Generalized Projection
- Aggregate Functions
- Outer Join

Generalized Projection Allows Computed Values to be Projected.

- Allow projections to include computations based on column/attribute values in addition to column values themselves
- Example: List the call numbers of all overdue books, together with the number of days they are overdue.
- $\pi_{call_number, today date_due} \sigma_{date_due < today} checked_out$

Aggregate Functions Give Summaries of Multiple Rows.

- Allow the use of functions which return summary data from a set of rows/tuples
 - min, max, sum, average to a column/attribute
 - count to an entire table/relation
- Denoted by the fancy capital G
- Example: What is the average salary of all employees?
 - G _{average(salary)} employee
- Can produce summaries by groups
- Example: Print a list of borrower id's and the number of books each has out

• borrower_id G count(call_number) checked_out

Outer Join Returns Rows That Do Not Necessarily Have a Match.

- Variant of natural or theta join which will include rows/tuples in one table/relation, even if there is no match in the other
 - Includes a dummy relation of all nulls in the result row for the unmatched relation
 - Variants
 - Left outer join denoted by \bowtie -- no match in right table OK
 - Right outer join denoted by ⋈ -- no match in left table OK
 - Full outer join denoted by \bowtie -- no match in either table OK
- Example: List the titles of all books, together with the borrower id of the person (if any) who has the book checked out.
 - $\pi_{borrower_{id, title}} book \bowtie checked_out$

Homework 1