CS211 Lecture: Quality Assurance

Last revised October 2, 2008

Objectives:

- 1. To define key terms: "failure", "fault", and "error"
- 2. To introduce and distinguish between black box and white (glass, clear) box testing.
- 3. To discuss the process of choosing test cases, including the notion of equivalence classes and path, edge, and node (statement) coverage.
- 4. To introduce and distinguish between unit, integration, acceptance, and regression testing.
- 5. To introduce and distinguish between top-down, bottom-up, and "sandwich" testing, and to introduce the notion of test "scaffolding".
- 6. To discuss testing, inspection, and formal verification as alternate and complementary means of attempting to ensure program correctness.
- 7. To introduce the process of reasoning from preconditions & invariant to postconditions and invariant.
- 8. To review the use of loop invariants

Materials

- 1. Projectable+Demo of old version of SimpleDate using a test driver main method
- 2. Demonstration of JUnit test of SimpleDate (NetBeans project) two versions of the project one without JUnit test to demonstrate creation; other with complete JUnit tests
- 3. Demonstration of JUnit test of GUI

I. Introduction

- A. In our study of the software lifecycle, we have seen that one of the major activities is quality assurance (or verification and validation).
 - 1. While we are covering this as a distinct topic in the curse, it is important to note that quality affects every aspect of the software lifecycle it is not an add on at the end of the process. Most of what I will say in this series of lectures pertains to quality assurance in general regardless of where in the lifecycle it is actually done.
 - a) A key principle is that the earlier an error is discovered, the less expensive it is to fix - often by as much as an order of magnitude or more.

For example, suppose the requirements for a piece of software contain an error. Fixing the defect in the requirements is clearly a lot easier than if the software, after being written to fulfill the erroneous requirements, now has to be changed to do what is should have done in the first place.

(An example of this from a different realm - recently a contractor came out and put new gutters on my neighbors house. Alas - they had the wrong street address - she hadn't contracted for any work on her house by them! The result was that she got a free set of gutters!)

- b) Nonetheless, it is common for extensive effort to be expended on verification and validation at the end of the software lifecycle, which is why we consider this topic here.
- 2. It is not uncommon for testing (and fixing the errors that testing uncovers!) to represent half or more of the time (and hence half or more of the cost) of initial development of a software product. Obviously, then, this aspect of program development is a prime target for savings.
 - a) Unfortunately, in practice, savings are often achieved in this area by shortcuts that result in products being delivered that do not do what they are supposed to do, or produce "blue screens" or other unpleasant phenomena. Clearly, this is not an ethical or professional approach to developing software.
 - b) We can save testing and error correcting effort legitimately by approaching it in a correct way which is the focus of this series of lectures.
- B. Before going further, we need to be sure we are clear about several related terms that are often used interchangeably, but really have distinct meanings: "failure", "fault", and "error".
 - 1. Failure refers to an observable incorrect behavior of a system. A failure may be as minor as an appearance problem in a GUI, or it may be that the software causes they system to crash.
 - 2. A fault is something that is wrong with the software. All failures are caused by faults, but not all faults manifest themselves as failures at least during testing.
 - 3. An error is the mistake the caused the fault. Faults exist because of errors but it is possible for an error to not result in a fault. (E.g. most of us have made driving errors that have not resulted in collisions.)
 - *EXAMPLE:* Consider the following java code, which is supposed to calculate the average of all the elements in an array of floats: x:

```
float sum = x[0];
for (int i = 0; i < x.length; i ++)
    sum += x[i];
System.out.println("The average is " + sum / x.length);</pre>
```

a) What's wrong with this code segment?

ASK

For some reason, the programmer included x[0] in the sum twice. Either the initialization should have been sum = 0, or the for loop should have started at 1. If the programmer intended the latter, then the error was carelessness in typing the initial value for i in the loop.

- b) In any case, the fault in this software is that it calculates the average incorrectly by counting x[0] twice.
- c) The failure that would result from this fault is that an incorrect average is printed to System.out.
- d) Would this code always result in a failure (an incorrect average being printed?)

ASK

No - not if x[0] happens to be zero! (or is so small, relative to the overall sum, that counting it twice doesn't produce a noticeably wrong result.)

Nonetheless, a fault is present, whether or not it results in a failure.

- 4. Note that catching exceptions and dealing with them appropriately does not demonstrate a fault in the software on the contrary, quality software anticipates things that can go wrong in "the outside world" and is prepared to cope with them.
 - a) Most legitimate exceptions arise from external problems such as a communication link failure or another computer system being down or a file not existing on disk or a human error in typing input.
 - b) However, it is very bad practice to try to cover up exceptions that arise from faults in the software e.g. code like the following might prevent a failure, but at the cost of hiding a fault:

```
try
{
    // Some code
}
catch(Exception e) // Catches any exception
{ } // and simply ignores it
```

C. Quality assurance has, as its first goal, the <u>prevention</u> of errors. Given that this is not 100% possible, the second goal of quality assurance is to find and remove faults. Thus, quality assurance activities like inspection and testing are successful just when they find faults - not when they fail to find faults!

(Consider the process you go through of testing a program before you turn it in. The testing process is actually successful if the faults cause visible failures that you can fix. Having the software appear to work correctly - even though it contains faults - is not success at this point!)

- D. There are three broad categories of quality-assurance activities.
 - 1. Testing
 - 2. Inspections
 - 3. Formal Proof of Correctness

II. Execution-Based Testing

- A. In this section, we will focus on what is sometimes called "execution-based testing" i.e. running the software (or a portion of it) under controlled conditions and identifying failures. Execution-based testing, of course, can only take place during or after the implementation portion of the software lifecycle (though there has been some interest in the notion of "executable specifications" that would allow this kind of testing earlier in the process).
- B. All too often, testing is approached as follows: we write code that we think is correct, and then we test it with data for which the correct results are known. When discrepancies are found, we locate their source and repeat the testing procedure until all tests produce correct results.
 - 1. But does this process really mean that we have succeeded in producing correct software? NO it simply means we have succeeded in producing software that correctly handles all of the cases we have anticipated.

a) Note that many serious errors have arisen precisely because the developers of a system did not anticipate some possible input when specifying and designing the system. It is not surprising that, in such cases, no test data showed the fault.

EXAMPLES: Y2K; rising moon in NORAD's first missile warning system

- b) Of course, no system can totally prevent such situations from arising. The fact that they have occurred should keep us from overconfidence in software that "passed all the tests".
- 2. Does this process give us confidence in the correctness of our software? NO because each time we find an error we begin to wonder what others might be lurking out there undetected.
 - a) Harlan Mills put it this way:

"There is no foolproof way ever to know that you have found the last error in a program. So the best way to acquire confidence that a program has no errors is never to find the first one, no matter how much it is tested and used." (In 'How to Write Correct Programs and Know it').

b) One textbook author spoke of what he called "the law of conservation of bugs":

"The number of bugs remaining in a large system is proportional to the number of bugs already fixed. In other words, a fault-ridden system will always tend to remain a fault-ridden system. This is because a poorly-designed system will not only have more faults to start with, but will also be harder to fix correctly and hence will suffer more strongly from the ripple effect." (The phenomenon that fixing one fault often introduces another.)

- 3. When testing is done by the same person who wrote the software, a third problem also comes into play: a psychological one. Since we really hope our software is correct (and we don't want to have to rework it again), it's easy for us to not test it as rigorously as we should
- 4. As we noted earlier, waiting until the code is all written before testing it means that correcting some kinds of errors will be very costly.

- a) If the software specifications were wrong, and this isn't discovered until it is tested, then the whole piece of software may have to be rewritten virtually from scratch!
- b) Thus, effort is conserved if we try to ensure correctness at every step along the way, rather than waiting to test the finished product.

C. Choosing good test data is critical - but is often the hardest task of all.

1. Ideally, we would like to test our software EXHAUSTIVELY - i.e. by testing every possible input. But if we could do that, we probably wouldn't need to bother writing the program!

EXAMPLES:

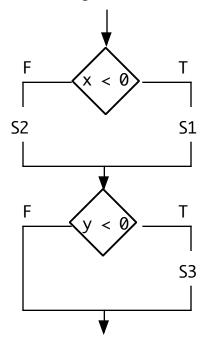
If a program accepts a single integer as input, there are 4 billion possible cases that might need to be considered!

Even if the values it accepts are limited, they can interact - e.g. a program that accepts 5 integers in the range 1..10 actually has 10⁵ or 100,000 possible cases

- 2. We are therefore forced to use only a small subset of the possible inputs for testing. How we choose this subset depends in part on whether we are doing black box or white (glass, clear) box testing.
 - a) Black box testing is done without regard to any knowledge of the internal structure of the software. Test cases are chosen only on the basis of the specifications. We will say more about choosing cases for black box testing shortly.
 - b) White box testing (also known as glass or clear box testing) is done by choosing cases based on the code, with an attempt to achieve some sort of "coverage" of all portions of the code.
 - (1) Statement coverage we ensure that every statement is tested by at least one test case. (The text author calls this "node coverage".)
 - (2) Path coverage we ensure that every possible path through the program is taken. (This necessarily implies statement coverage) Of course, for programs containing loops, this is impossible, since there are infinitely many possible cases.
 - (3) Edge coverage we ensure that every possible edge in the program graph is taken at least once. (A practical alternative to path coverage.)

(4) EXAMPLE: The following is a highly-simplified example to illustrate the difference. Consider the following block of code, where the "S"'s are arbitrary statements that don't affect the value of x or y:

This corresponds to the following flow graph



(a) To achieve statement coverage, we need to ensure that each statement (S1, S2, S3 and the if tests) is executed at least once. This can be done with just two sets of test data. Can anyone see a way to do this? (Actually there are lots of possibilities)

ASK

i)
$$x = -1$$
, $y = -1$ (tests S1, S3 and ifs)
ii) $x = 1$, $y = -1$ (adds S2)

(b) To achieve edge coverage, we need to ensure that each of the edges in the graph is traversed at least once. The above data set misses one edge. Which one?

ASK

The "false" edge out of the second test (s < 0).

We could achieve edge coverage by adding a data set like x = 1, y = 1. (For that matter, in this case we could change the second original data set to this as well)

(c) To achieve path coverage, we need to ensure that each possible path through the program is executed. How many possible paths are there?

ASK

Four (two possibilities for x) * (two possibilities for y)

For example, the following data would test all paths:

```
i) x = -1, y = -1 (right, right)
ii) x = -1, y = 1 (right, left)
iii) x = 1, y = -1 (left, right)
iv) x = 1, y = 1 (left, left)
```

- (5) In practice, statement coverage and edge coverage are both possible and edge coverage is preferable since it implies statement coverage. Path coverage, however, is often not practical, due to the large volume of cases that might be needed.
 - (a) Example: a program has 10 inputs, each of which selects one of two paths at a branch in the program. There are potentially 2^{10} (=1024) paths. With 20 variables, this jumps to over 1 million.
 - (b) A single loop can generate a near-infinite number of possibilities. Example:

```
int x;
while (x > 0) {
   if (x == 3)
        S1;
   else
        S2;
   x = x / 2;
}
```

Possible paths include the following, all of which differ:

```
x = 0 (nothing)

x = 1: S2

x = 2: S2, S2

x = 3: S1, S2

x = 4: S2, S2, S2

x = 6: S2, S1, S2
```

•••

And so on for infinitely many possibilities (or at least as many as there are possible values of x represented by an int on the underlying machine)

- c) Commonly, testing done during development uses a clear box approach, while final acceptance testing is done using a black box approach.
- 3. For clear box testing, we choose test cases that achieve the kind of coverage (typically statement or edge) we are trying to achieve.
- 4. In identifying test cases for black box testing, it is helpful to realize that the set of all possible data the program can handle (which is often large if not infinite) can be partitioned into equivalence classes.

EXAMPLE:

Suppose one input to a program must be an integer in the range 0..100. Suppose the program is supposed to do some computation with the valid integers, and to print an error message for an invalid integer.

The equivalence classes are: negative integers, integers between 0 and 100 (inclusive) and integers greater than 100.

- a) For each equivalence class, we want to be sure that our test data includes
 - (1) A typical input from the class (e.g. 20 or 50 or 98 would be suitable for the class of integers in the range 0..100)
 - (2) If the class represents valid input, boundary inputs values that lie right on the edges of the class e.g. for integers in the range 0..100, the boundary values would be 0 and 100.

- (3) If the class represents invalid input, values that are barely illegal (just on the wrong side of the boundary) e.g. -1 for the class of negative integers and 101 for the class of integers > 100.
- b) A common error I have noticed in student test plans is to expend a lot of effort on all sorts of illegal input (including really bizarre possibilities) while not testing correct input at all, or in only a very limited way! The result is that we have confidence that the program can handle the bizarre nicely, but no confidence that it will do the right thing in the normal case!)
- 5. Because the author of a piece of software is not necessarily the best person to test it, some organizations have a separate "Software Quality Assurance Group" to do testing. In this case
 - a) Software authors may clear-box test their software before releasing it to the QA group.
 - b) The QA group will black-box test it based on the original specifications.
 - c) Doing things this way helps prevent the possibility that a software author didn't think about how the program would handle a certain piece of anomalous input, so his/her test data never tests it!
- D. Execution-based testing needs to take place at several points during and after the implementation process.
 - 1. One approach to testing (which I am not advocating) is called the "big bang approach". It goes like this: write all the code, and then when everything is written, test it
 - a) This is a common method used by introductory CS students
 - b) It usually leads to chaos when applied to large programs. When something goes wrong, where do you look?
 - c) The other approaches are therefore much to be preferred!
 - 2. Software of any size should be tested by using a combination of UNIT TESTING and INTEGRATION TESTING, followed eventually by ACCEPTANCE TESTING
 - a) Unit testing means testing each piece of the software individually when it is coded to ensure that it performs its part of the overall computation correctly.

Note that unit testing can (and should) take place as the software is being written.

- b) Integration testing means testing as the various units are put together into larger pieces or a complete program
 - (1) If every component has been successfully unit-tested, then any remaining errors should be interface errors cases where a caller of a method made different assumptions about what the method does than the author of the method assumed.

EXAMPLE:

Suppose a certain method is required to compare two objects and return true or false based on their relative order in a sorted list. Assume this method is used by another method that actually sorts the objects.

Suppose the author of the method understands the expectation to be that the method returns true if the *first* object belongs *before the second*, but the author of a sorting method that uses it assumes that it returns true if the *second* object belongs *before the first*.

Both methods would test successful during unit testing (based on their author's understanding of the interface between them.) However, the error would show up in integration testing with the output being backwards!

- (2) Integration testing is often a crisis time in software development but need not be if the preconditions and postconditions of methods are spelled out carefully before coding begins. (As we discussed in connection with implementation.)
- (3) In a large system, integration testing can occur at many levels, as larger and larger pieces of the final system are integrated with one another.
- c) Acceptance testing is performed by the customer before "signing off" on the finished project.

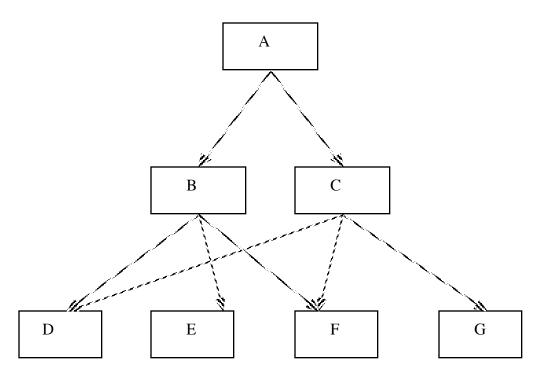
Sometimes formal acceptance testing is preceded by "alpha testing" and "beta testing". (The cynic in me can wonder how much commercial software that one buys is really only at beta level - or below!)

- 3. Because fixing one problem with a piece of software often introduces another problem, there is also a need for REGRESSION TESTING. This involves repeating tests that have already succeeded after every change to be sure that the software still works correctly.
- E. One question that arises in this context is "how can I do unit testing or even integration testing of software that depends on other code that hasn't yet been written?"
 - 1. We have to develop classes in some order, and therefore must be able to test one class while other classes have not yet been written. This complicates testing because we get into a "chicken and egg" problem.

EXAMPLE:

Suppose a method mA of class A uses a method mB of class B. Suppose further - as will often be the case - that mA produces some output that is visible to the user (and thus can be examined during testing), but mB produces no directly visible output. Which class should we implement and unit test first?

- a) If we try to implement class A first, then when we try to test mA we run into a problem because it relies on mB, which has not yet been written.
- b) If we try to implement class B first, then when we try to test mB we run into a problem because it produces no visible results the results of mB are only visible when it is called by mA, which has not yet been written.
- 2. In general, there are two broad approaches to the question of "in what order do we implement the classes", called TOP-DOWN and BOTTOM-UP. We can see where these names come from if we arrange the classes hierarchically, so that each class only depends on (makes use of the methods of) classes below it in the hierarchy so we get something like this:



(actually, this kind of strict hierarchical structure is more common in non-OO systems than in OO systems, which tend to have more cooperating peers. Even so, though, it is often good practice to arrange the objects in an OO system in layers).

- a) In a top down approach, we might implement and unit test modules in the order A, B, D, E, C, F, G.
- b) In a bottom up approach, the order might be D, E, B, F, G, C, A.
- c) Also possible (and useful in many cases) is a "sandwich" approach in which we first do the "bread" (A, D, E, F, G) and then the "filling" (B and C). (This approach is common if the highest layers are the GUI and the lowest layers provide utility services like access to a database, with the middle layers being the business logic.)
- 3. Whichever order of implementation and testing we choose, we are forced to create some extra code just to allow us to perform testing. This code is often called scaffolding by analogy to building construction,, where temporary structures (scaffolds) are built to allow work on the target structure.
 - a) Consider the matter of unit testing a method that relies on another method not yet written as would happen in the above if we chose to develop A first (or for that matter to develop B or C before developing D, E, F, and G.) In this case, one must write a STUB -

a piece of code that stands in for the as-yet unwritten method by doing something reasonable, like simply printing out the fact that it was called or returning a known "dummy" value.

Example: In the skeleton code I gave you for the first registration system lab, all of the method prototypes were present, mostly with empty bodies. In the case of a method that returns a value to its caller, a dummy return statement (labeled STUB) was inserted to return an acceptable value (typically null).

Note: to thoroughly test a method that relies on stubs for other methods, the stubs would have to be able to produce a full range of possible results (which may mean interactively asking the user to specify a particular result). E.g. in the registration system lab, a complete stub for the getCourse(String id) method of class Database would have to ask the user whether it should return null (as it now does) or an arbitrary valid course.

- b) Now consider the matter of unit testing a method before its caller has been written as would happen in the above example if we chose to develop D, E, F, or G first (or to develop B or C before developing A). To do this, it is necessary to write a piece of "throwaway" code called a TEST DRIVER to call the method under test with various inputs and report its results.
 - (1) One approach is to create a separate program that performs the testing by requesting input from the user (or providing some constant input), calls the method under test, and then either reports the result or checks the result against a known good value. In Java, this can often be incorporated into a class as a main method that serves to exercise that class. (A Java program can have main methods in any number of classes one is designated as the main method for the program when it is run and the rest are ignored.). Thus, a Java class that is not a main class could still have a main method which serves as its test driver.

EXAMPLE: An earlier version of the SimpleDate.java class I gave you for the project incorporated the following test driver (PROJECT)

```
public static void main(String ☐ args)
 SimpleDate today = SimpleDate.getToday();
 SimpleDate tomorrow = today.daysLater(1);
 SimpleDate aWeekFromNow = today.daysLater(7);
 System.out.println("Today is " + today);
 System.out.println("Tomorrow is " + tomorrow);
 System.out.println("A week from now is " +
     aWeekFromNow);
 System.out.println("A week from now is " +
     aWeekFromNow.daysAfter(tomorrow) + " days
     after tomorrow");
 System.out.println("Today equals tomorrow: " +
     today.equals(tomorrow));
 System.out.println("Today is after tomorrow:
     today.isAfter(tomorrow));
 System.out.println("Tomorrow is after today:
     tomorrow.isAfter(today));
 // Unless the program is started a few seconds
 // before midnight, the newly constructed object
 // should test the same as today
 try { Thread.sleep(10000); }
 catch(InterruptedException e)
  { }
 SimpleDate tenSecondsLater = new SimpleDate();
 System.out.println("Ten seconds later equals " +
     "today " + tenSecondsLater.equals(today));
 System.out.println("Ten seconds later is after "+
     "today " + tenSecondsLater.isAfter(today));
 // Now test the code for diddling with today
 SimpleDate.changeTodayBy(5);
 System.out.println("After diddling with the " +
     "date, today is " + SimpleDate.getToday());
```

}

With this code in place, it was possible to run the class as if it were a standalone program, and then manually examine the output to see if all the methods were doing the right thing.

(DEMO)

(2) In the Java world, there is an approach to testing called JUnit. In this approach, one develops automatic testers in parallel with the code - typically one test method for each (non-trivial) actual method. The purpose of the test method is to ensure that the method being tested appears to work correctly (i.e. that it is not "broken"). There is a framework that supports automatically running all the testers and reporting success or failure without requiring manual inspection of output; this can be done after any change to ensure that it did not break something.

EXAMPLE: The current version of SimpleDate

- Open project with complete JUnit test
- Show code for SimpleDateTest
- Run it
- Demo what happens when a test fails (delete result.add ... line from daysLater())
- Open project without JUnit test
- Show NetBeans option for generating a test class
- -Open project with tests and show testing of GUI (note need to interact)
- (3) Note that it is usually only necessary to develop one or the other type of scaffolding. Once we have tested a method that relies on stubs for as-yet unwritten methods it calls, we can use it to help us test those methods when they are written. Conversely, if we have tested a method using a test driver, we can then use it to help us test the methods that call it.
- c) Object-oriented testing is a still a significant research area. A key question that is not yet fully answered is how best to test a class in isolation (as a unit) when classes are designed to work together.
- F. When errors are uncovered during testing, we must, of course, locate and correct them a task that is often easier said than done!
 - 1. This task is made easier if we are disciplined about unit testing and integration testing, since the amount of code we must consider when looking for the error is kept down.

- a) During unit testing, we must of course only consider the unit being tested (or perhaps the test driver!)
- b) During integration testing, we can focus our attention on the INTERFACES between the previously tested units.
- 2. One tool that can often be used to help us here is one that is commonly (but perhaps erroneously) called a SYMBOLIC DEBUGGER.

(We worked with this kind of tool in lab 3)

- G. Finally, it should be noted that effective testing calls for a TEST PLAN. A TEST PLAN must address issues like:
 - 1. Scaffolding that needs to be built
 - 2. Testing procedures including the order in which various tests are done.
 - 3. The test suite the actual data to be used. Wherever possible, it is good to put the test suite into some form that it can easily be run again during integration testing preferable an electronic form where applying the test suite can be automated; otherwise paper form.

III. Inspection

- A. While testing will always be one part of the process of attempting to ensure program correctness, best results are achieved when testing is used in conjunction with other methods. We will look at a number of methods that are based on disciplined READING of the code and REASONING about it:
- B. Desk-checking: careful reading of our work ourselves, to try to uncover places where it is not correct and (ultimately) to convince ourselves that it is correct once faults have been removed.
- C. Inspections/reviews: having others read our work to help locate faults.
 - 1. Because we know what we meant to do, we will sometimes fail to see places where we didn't actually SAY what we MEANT. Someone else may catch this for us.
 - 2. Inspection and review can be done in many ways.
 - a) Informally by asking a colleague to review our work. (This approach can be used very productively when doing a project with a partner.)

- b) Various forms of Structured Walkthroughs are often used in industry. A small group of an author's peers will listen as he/she walks through the logic of his/her work with them, pointing out things they see that need correction or improvement.
- c) Formal reviews by management.
- 3. An interesting fusion of the these two approaches (desk-checking and reviews) that has arisen recently is the idea of PAIR PROGRAMMING, which is the idea behind the way we structure labs in the course, and behind assigning team projects. However, having two people working independently on the same project is not pair programming; pair programming means two people ALWAYS WORKING ON EVERYTHING TOGETHER. (One types; the other thinks and interacts.)

IV. Basic Concepts of Formal Verification

- A. Formal verification means applying the methods of mathematical proof to programs in order to PROVE a program correct. Note that while testing only gives RELATIVE confidence in a program's correctness (unless of course you can test every possible input), a mathematical proof can give ABSOLUTE confidence provided its logic is correct.
 - 1. The method of program proof is not a total substitute for testing since there can still be flaws in our proof logic. (There is a famous example in the software engineering literature concerning a short program that was "proved" correct several times but each time it contained a fault which was not caught due to an error in the logic of the proof!)
 - 2. But when formal verification is coupled with testing and inspections it can give a very high degree of confidence in program reliability.
 - 3. Using the methods of mathematical proof while one is developing a program can help to prevent errors in the first place by helping us think clearly about what we are doing.
 - 4. In practice, there are serious limitations to the usefulness of this approach due to the time and effort involved. However, in critical, tricky portions of a program or systems where human lives are at stake (e.g. airplane flight control software) it can be a powerful aid.
- B. By formal verification, we mean using the methods of mathematical proof to demonstrate that code MUST be correct.

1. The starting place of formal verification is the preconditions, postconditions, and class invariants we identified during detailed design and implementation.

2. Recall that:

- a) A precondition of a method is an assertion that describes conditions that the caller of a method must guarantee will hold when the method is called.
- b) A postcondition of a method is an assertion that describes conditions that a method guarantees will hold when it terminates, provided it was called with its preconditions satisfied. (No guarantees if the preconditions don't hold!)
- c) A class invariant is an assertion that holds:
 - (1) When an instance of the class is first constructed.
 - (2) After the COMPLETION of every public method (that is called legally i.e. with its preconditions satisfied)
 - (3) Note that the invariant can become false <u>during the execution</u> of a public method, so long as the method guarantees to make it true again before it completes.
 - (4) The invariant need not hold for private methods, since these can only be called by public methods, which are allowed to make the invariant momentarily false as long as they finish with it true.
- 3. As a consequence, every public method of the class can assume that the class invariant holds when it is called, along with the preconditions.
- C. In formal verification, we prove the correctness of each public method by showing all of the following:
 - 1. If the method is called with its preconditions satisfied, and with the class invariant holding, then it will guarantee upon completion that its postconditions are satisfied.

```
Symbolically::
{ pre & inv } M { post }
```

2. If the method is called with its preconditions satisfied, and with the class invariant holding, then it will guarantee upon completion that the class invariant remains satisfied.

Symbolically: { pre & inv } M { inv }

- 3. If the method is called with its preconditions satisfied, and with the class invariant holding, then we must also ensure that every method it calls has its preconditions satisfied as well (and the class invariant as well if it is a public method)
- D. Note that, in order to prove the correctness of a public method, we may also need to prove the correctness of any private methods it calls. A private method is proved true by showing that, if it is called with its preconditions satisfied, it guarantees the truth of its postconditions with no assumptions about the class invariant unless explicitly stated in pre/post conditions.
- E. In developing a proof of a method, we are allowed to rely on:
 - 1. General properties of the various statements comprising its body.
 - 2. The correctness of methods it calls i.e. if our method can guarantee to satisfy the preconditions of any method it calls, then it can rely upon the postconditions of that method as part of establishing its own correctness.
- F. Example: Coffee Can problem (handed out earlier).
 - 1. Did anyone discover the relationship between the initial state and the color of the final bean?

ASK

2. What condition do we need to add to the invariant to help us prove this conclusion?

ASK

3. Discuss each public method - showing

{ Pre & Full inv } M { Post & Full inv }

Note that the class invariant: $w \mod 2 == w_0 \mod 2$ is <u>not</u> satisfied when chooseBean() is called the second time in playOneRound() because the code just before may decrement w. This is OK, because

chooseBean() is a private method and does not require this in its preconditions.

G. Last semester, we introduced related concepts called a LOOP INVARIANT and LOOP TERMINATION.

1. What is a loop invariant?

ASK

A loop invariant is an assertion that is known to be true the first time the loop body is entered, and whose truth is not altered by a complete execution of the loop body.

EXAMPLE: In this problem, we construct an instance of the CoffeeCan outside the loop, and perform operations on it inside the loop. Since the class has an invariant, this is also part of the invariant for the loop.

- (1) The class invariant is made true when the CoffeeCan is constructed.
- (2) Each time through the loop, we call playOneRound(). The precondition of playOneRound() is guaranteed by the loop condition. Therefore, the class invariant is preserved by each call to playOneRound().

(Note: if we slightly changed the loop header from > 1 to >= 1, we would no longer guarantee the precondition of playOneRound(), in which case the class invariant would not be guaranteed to be preserved by the loop!)

2. Termination of Loops

a) When proving the correctness of a loop, there is one other item we must consider: TERMINATION. We need to show that the loop will eventually terminate.

b) EXAMPLE:

In this problem, the postcondition of playOneRound() is that the number of beans in the can will be reduced by 1. Thus, we are ensured that the loop will terminate, because the number of beans must eventually fall below 2.

3. The combination of type declarations, method postconditions, the loop invariant and the loop termination condition allows us to prove the correctness of our conclusion about the coffee can problem:

- a) The number of beans in the can is an integer. (Type declarations)
- b) We start out with > 1 beans in the can, and there is a nonnegative number of beans of each type. (Constructor postcondition)
- c) Each time through the loop reduces the number of beans by 1. Thus, it must eventually fall to exactly one.
- d) The loop invariant ensures that neither bean count can go negative; therefore, we have exactly one bean of one color and no beans of the other at this point.
- e) This satisfies the precondition for finalBeanColor()
- f) The additional invariant condition guarantees our final result.